**Chapter 1**

**Introduction**

**1.1 Sign Language**

The World Health Organization (WHO) estimated that, 250 million people in the world are deaf as well as dumb. [1] These group people of use symbolic language to communicate with other people. This symbolic language is called sign language. Sign Language is a build for communication used worldwide among hard of hearing, and deaf peoples. Sign language is not a unique language signed consistently in different countries. Sign language is not recent improvement. There is proof that speaking through gestures has been around since the start of human development [20]. Different counties have their own sign language such as American Sign Language, French Sign Language, Indian Sign Language and Puerto Rican Sign Language to name a few. Table 1 give information about different sign languages used in western continent. Gesture based communication is dependent on region and has significant differences from other languages. It is very important to understand sign language when we communicate with deaf or young children and their families. Lack of understanding result in significant challenges in understanding this community and may result miscommunication.

Table 1: Sign Language in the Americas [20]

|  |  |  |
| --- | --- | --- |
| **North America** | **Central America** | **South America** |
| •American Sign Language  •Inuit Sign Language  •Quebec Sign Language  •Puerto Rican Sign Language | •Costa Rican Sign Language  •Guatemalan Sign Language  •Honduras Sign Language  •Mayan Sign Language  •Mexican Sign Language  •Nicaraguan Sign Language  •Panamanian Sign Language  •Salvadorian Sign Language  •Tijuana Sign Language | •Argentine Sign Language  •Bolivian Sign Language  •Brazilian Sign Language  •Chilean Sign Language  •Colombian Sign Language  •Ecaudorian Sign Language  •Paraguayan Sign Language  •Peruvian Sign Language  •Uruaguayan Sign Language  •Venezuelan Sign Language |

Sign Language is a language which is used to convey messages by hand movements, facial expression and body language for communication. It is mainly used by deaf and people who can hear but cannot speak. Sometime family members and relatives must learn sign language to interpret which enables deaf and wider communities to communicate with each other.

**1.2 Mythologies and Misunderstandings about Sign Language**

The Sign language is enclosed by many mythologies and misunderstanding. Most people who are not disable think that Sign language is just simple a manual representation of the spoken language which is not true. In fact, our language and sign language of the deaf have little in common. Sign language has the difficulty of the verbal language, but it is self-determining from the alphabets. The best example is British Sign Language and American Sign Language which are meaningless although the facts show that disable people from United States and Britain perfectly understand each other.

Another common misunderstanding about sign language is that it is globally understandable which is of course not true. As explained above, the Sign language that is used by the deaf in Unites States and Britain are not the same. The different sign languages might be similar in some alphabets but a deaf person from one country to country communicate as fluently as hearing people from the two countries.

Since sign language is a language of its distinct language, finger spelling or the use of guidebook alphabet cannot be used as an alternative to sign. It is utilized in marking the words with a non-existent sign or when the sign isn't known. In addition, Deaf person would take hours to convey a few minutes of messages through finger spelling.

**1.3 Objective:**

My main objective of my thesis is to help deaf community to increases their self-esteem and IQ level and improve their communication skills. Students who are deaf or have a deaf parent or have a close relative with deaf individual will learn by themselves about sign language alphabets and numbers. Deaf community will learn their first step towards the American sign language. Although correct usage of sign gesture plays very important part in effective communication, deaf students are also encouraged to establish connection to deaf community and to carry their new knowledge and skill beyond the class room and into the community at large. Some of important objective are discussed in Chapter 3.

**1.4 Methodology**

In this thesis, Image classification and machine learning have been used for Interpreting American sign language. For image classification, computer vision algorithms were used to capture images and to process data set for filtering as well as reducing noise from images. Finally, data set is trained Sign machine learning algorithm, conventional neural network for measuring accuracy of training data set, result of thesis algorithm is explained in chapter 7. The abstract view of the derived approach combining the image classification and machine learning for American sign language is shown in Figure 1.

Feature Vector

Prepare Image

Feature Extraction

Neural Network

Feature Extraction

Convert RGB to GRAY

Classification

Apply Threshold/Edge Detection

Classified Image

**Figure 1: Project overview for American sign language**

**1.5 Outline:**

**Chapter 2**

**2.1 Related Work**

**2.1.1 American Sign Language using Machine Learning**

American sign language recognition is not a new machine learning problem. During recent decades, different researches already worked on different classifiers such as linear classifiers, neural networks and Bayesian networks [2-11].

As per research point of view a linear classifier is easy to work with because linear classifier are relatively simple models, it requires sophisticated feature extraction and preprocessing methods to get good results [2, 3, 4]. Singha and Das [2] achieved an accuracy of 96% on Ten classes for images of gestures of one hand using Karhunen-Loeve Transforms. These translate and rotate the axes to build up a new framework based on the variance of the data. This technique is useful after using a skin color detection, hand cropping and edge recognition on the images. They use a linear classifier to recognize number sign including thumbs up, first and index finger pointing left and right, and numbers only. Sharma [4] has done research using Support Vector Machines (SVM) and k-Nearest Neighbors (KNN) to illustrate each color channel after background noise deletion and noise subtraction [4]. Their research suggests using contours, which is very useful to represent hand contours. They got an accuracy of 62.3% using a Support Vector Machines on the segmented color channel model.

Machine learning is most commonly used for image recognition. Hidden Markov Model (HMM) and Dynamic Time Warping (DTW), two kinds of machine learning methods, are widely applied to achieve high accuracies [5, 6, 7]. These are mostly good at capturing time-based patterns, but they require clearly characterized models that are defined before learning. Starner and Pentland [5] used a Hidden Markov Model and a 3-Dimesional glove that detect hand movement. Since the glove can attain 3-Dimesional detail from the hand regardless of spatial orientation, they achieved the best accuracy of 99.2% on the test set. Using Hidden Markov Model uses timeseries data to track hand actions and classify based on the position of the hand in recent frames.

Suk [6] suggested a system for detecting hand gestures in a continuous video stream using a dynamic Bayesian network or DBN model. They try to classify moving hand gestures, such as creating a circle around the body or waving. They attain an accuracy of nearly 99%, but it is worth noting that all hand gestures are different from each other and are not American Sign Language. However, the motion-tracking feature would be applicable for classifying the dynamic letters of ASL: j and z.

Artificial Neural networks (ANN) have been used to capture American Sign language transformation [8, 9, 10, 11]. Possibly, the most important advantage of artificial neural networks is that they represent the most important classification structures.However, ANN require significantly more time and data to train. Up to the present time**,** most have been comparatively low.Mekala [8] classified video of ASL alphabet into text using unconventional feature abstraction and a three-layer Neural Network.They extracted features using hand situation and movement.In the past, American sign language classification, could recognise the presence and position of 6 “points of interest” in the hand, each finger and the center of the palm. Mekala also used Fourier Transforms of the images to classify what section of the frame the hand is positioned in.Whereas they claim correctly categorize 100% of images with this framework, there is no indication of whether this result was reached in the training, validation or test set.

Admasu and Raimond [9] classified Ethiopian Sign Language and achieved 88.5% accuracy result using a feed Forward Neural Network.They use a substantial amount of image preprocessing, including image size standardization, image background deduction, contrast adjustment, and image segmentation**.** Gabor Filter and Principal Component Analysis method was used to extract features.The most related work up to date is by L. Pigou’s [11] research of ANN’s to categorise 20 Italian gestures from the “ChaLearn 2014 Looking at People” gesture recognising competition.They used a Microsoft Kinect on whole body images of person performing the gestures and reach a cross-validation accuracy of 91.7%.With the 3-Dimensional glove, the Kinect allows detection of depth features, which helps significantly in classifying American sign language.

Non-Vision based technology such as Glove-based handshape recognition normally contains the person wearing glove and a certain quantity of wires to connect this glove to a computer. These methods are very hard and non-natural way to communicate with the computer [15]. This device required electricity or electromagnetic interference to get data about the hand, which is sufﬁcient to provide a description of a handshape gesture [16]. Scientists refer to data gloves in different ways, e.g. CyberGlove and Accele Glove.

Figure 2.1 shows the position of the sensors in a data glove proposed by Bedregal[17]. Basically, a timeline of frames can characterise any movement. Thus, a timeline of hand arrangement represents a hand movement using a data glove. An arbitrary generated hand conﬁguration was used to replicate the data transfer [17]. Each expression of the handshape is represented by a tuple of interval angles from each sensor. The detection was applied to Brazilian Sign Language (LIBRAS), using Fuzzy logic.

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**Figure: 2.1. A Data Glove design with Sensor.**

In this paper they developed a similar hardware device called the Accele Glove. In their research they used a microelectronic mechanical system (MEMS) to extract hand conﬁguration. They have been functional on Vietnamese Sign Language for twenty-three gestures with Fuzzy logic. They achieved the results by handshape, with an overall 98% precision. The relative angles between palm and finger is the data found from the sensing device. The glove covers six accelerometers and a BASIC Stamp microcontroller as in Figure 2.2[18-19].

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**Figure 2.2 A Glove device with Sensor**

Researchers [] have proposed a new system for a gesture-to-speech/text for deaf community, applied to Arabic Sign Language. This author includes the design and implementation of a smart glove. Main advantage of this glove is that it does not depend on light conditions, which means it gives good accuracy in dark environments. As per the author, the glove is low price, low power consumption and has full mobility. Another benefit of these gloves is that they attached ﬂex sensors which used a wireless interface to a microcontroller.

**Chapter 3**

**Data set**

**3.1 American Sign Language:**

American sign language [13] is used to communicate between deaf community and normal community. However, there are only 2.5 million ~ 5.0 million who speak sign language which significantly limits the number of people they can easily communicate with [12].



**American Sign language Manual Alphabet [13].**

American Sign Language is implemented from French sign language which was introduced by Thomas Hopins Gallaudet in United States [12]. ASL is like French sign language; individuals who speak American Sign Language can effectively communicate in French Sign Language. A variation of American Sign Language exits there are variations between English spoken in England, United States or Australia, there are differences in their sign languages [12].

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**Figure 1. American Sign language numbers. [13]**

**3.2 Characteristics of American Sign Language:**

* American Sign language is an entire visual-gestural dialect with its very own language structure, vocabulary, and linguistic structure.
* Like other sign languages, it utilizes the hands, the body, and face looks (counting mouth developments) to express significance and the eyes to see meaning.
* Hand - to-hand connection is especially critical in ASL since it has no composed frame. There are in any case, documentation frameworks that are utilized for recording signs on paper.
* ASL is separate from English and is unique from other sign languages. An example of the distinctiveness of sign languages from each other and from the surrounding spoken language(s) is that, although English is the shared spoken language of the U.S., Canada, and Britain, signers of ASL do not understand signers of British Sign Language (BSL).

**3.3. Statistics** **about sign language use in Canada:**

In Canada, Statistics Canada reports that as indicated by the 2006 Census 8,995 people revealed a gesture-based communication just like their primary language or one of their first languages, as given below.

**Table 1: Statics about Sign Language as a Mother Tongue [14].**

|  |  |
| --- | --- |
| American Sign Language | 2,485 |
| Quebec Sign Language | 730 |
| Sign languages, not included elsewhere | 5,780 |

In addition, Statistics Canada reports that as per the 2006 Census 43,090 people reported knowledge of a gesture-based communication, as provided below.

**Table 2: Statics about Knowledge of Sign Languages [14].**

|  |  |
| --- | --- |
| American Sign Language | 11,110 |
| Quebec Sign Language | 730 |
| Sign languages, not included elsewhere | 5,780 |

**3.4 Dataset and variables:**

I have created my own data set. This dataset was a collection of 36 characters which contain A to Z alphabets and 0 to 9 number digits. I used right hand to capture 1000 images for specific alphabets and numbers. Code was implemented to convert flip images to right to left hand image. The height and width ratios vary significantly but average approximately 50X50 pixels. The dataset contains over 72,000 images in grey scale color. Additionally, people can add their images to this dataset. Below figure shows an image of A to Z alphabet.

|  |  |  |  |
| --- | --- | --- | --- |
|  | **A** |  | **N** |
|  | **B** |  | **O** |
|  | **C** |  | **P** |
|  | **D** |  | **Q** |
|  | **E** |  | **R** |
|  | **F** |  | **S** |
|  | **G** |  | **T** |
|  | **H** |  | **U** |
|  | **I** |  | **V** |
|  | **J** |  | **W** |
|  | **K** |  | **X** |
|  | **L** |  | **Y** |
|  | **M** |  | **Z** |

**Figure 2: Data set images.**

|  |  |
| --- | --- |
| **Property** | **Description** |
| Alphabets | A to Z |
| Numbers | 0 to 9 |
| Color | Gray Scale |
| Dimensions | 50x50 |
| Height | 50 pixels |
| Width | 50 pixels |
| File type | JPEG |

**Table 3: Dataset Description and Image property**

**3.5 Capturing Images for Dataset**

To detect hand gesture using skin colour, there are different approaches including skin colour-based methods.In this thesis, after detecting and subtracting the face and other background, skin recognition and a contour comparison algorithm were used to search for the hand and discard other background colour objects for every frame captured from a webcam or video file.hand to extract their contours and saved the further for evaluation with the contours of the skin detected area of every frame.After detecting the skin area for each frame captured, contours of the detected areas were compared with the previously saved hand histogram template contours to remove other skin like objects existing in the image.If the contour comparison of the spotted skin area complies with any one of the saved hand histogram contours, then it captured hand gesture only.

**Chapter 4**

**Hand Gesture Detection**

**4.1 Introduction**

Object detection plays a very important role in my own dataset. To analyse and extract relevant data about an object of interest from an image, one needs to first get that object in the image. Hand posture detection refers to finding the place and size of hand within a sequence of images. Nowadays it is a very popular problem in computer vision problem and has many numerous applications, such as gesture recognition, sign language recognition, computer graphics games, and human-computer interaction (HCI).

Skin colour [21, 22, 23] is an important property to detect hand and tracking. However, Colour image has the different problem of removing other objects with similar colours such as face and human arm. To solve this problem, we introduce a new method to detect hand postures only using face detection and subtraction, skin detection, and hand postures contour detection and comparison algorithm [24]. The face was detection removed because the skin detection will detect the face and the face’s contours are very similar to the first-hand gesture contours. An interest of the area has been captured and another same skin colour has been removed from an interest of the area. After removing an unwanted area of the face, I detected the skin area using the hue, saturation, value (HSV) colour model since it has real-time performance and it is strong against alternations, scaling and lighting conditions. Then, the interested area of contours was compared with all the existing hand posture template contours to eliminate unwanted interest of area like objects existing in the image.

**4.2 Hand Detection Approaches**

There are different approaches for hand detection have been introduced in the literature that employs different visual features and, in many cases, their combination. These are different approaches such as motion, skin colour, shape, and 3D models of hands. Hand detection methods were discussed in [25] and will be discussed later in this chapter.

**4.2.1 Colour**

Skin colour detection has been used in many hand gesture recognition projects. The main objective of giving a model of skin colour is the choice of the colour space to be utilized. Different colour spaces have been introduced such as RGB, normalized RGB, HSV, YCrCb, and YUV. Colour spaces that effectively divide the chromaticity from the luminance parts of colour are typically regarded as preferable as I did in my approach by removing the Value (V) section in the HSV model. This is because of employing chromaticity-dependent mechanisms of colour only.

Generally, hull colour detection can be disordered by background objects that have a hull colour distribution like human skin colour. Some project has been done on this problem by using background subtraction [26, 27]. On the contrary, it was expected that unwanted background subtraction normally depends on the camera system that does not move with respect to a fixed background. Another solution [28, 29] has applied the dynamic modification of background compensation techniques.

**4.2.2 Shape Hand**

Shape property has been working to discover in frames. More details can be acquired by reducing the contours of objects in the frame. If the contour is perfectly detected, it provides a good presentation of the hand gesture which is indirectly related to a viewpoint, skin colour, and lighting. Typically, contour extraction based on edge recognition uses many edges fitting to the hand image area but also to distinct background objects.

Accordingly, sophisticated post-processing techniques are needed to develop the presentation of this method such as our approach in [24] by combining skin colour detection with contours detection and comparison after face subtraction. A second method that has been used in fingertip finding is pattern matching. Patterns can be images of fingertips [30] or fingers [31] or generic 3D cylindrical models [32]. These pattern matching methods can be upgraded by using extra image features such as contours [26].

**4.2.3 Learning Detectors from Pixel Values**

Currently, this technique that uses a machine learning method named posting has shown remarkably strong results in face recognition and good results in hand recognition [33]. In [34], an object recognition method was proposed in which a weak classifier may be a simple finder that uses basic image block differences efficiently calculated using an integral image. On the other hand, this technique may provide an unnecessary number of weak classifiers. The AdaBoost technique has a drawback because it does not consider the removal of chose weak classifiers that no longer take part in the recognition procedure. Also, there is some problem to distinguish the hand using the Viola-Jones method [34, 35] related to rotation and cluttered background.

**4.2.4 3D Model-Based Detection**

One major advantage of a 3D model-Based method is that it can allow for view-independent detection. The used 3D models must have enough degrees of freedom to adapt to the dimensions of the hand that exist in an image. Different mock-ups use different image features to build feature-model communications. Line and point features are applied in kinematic hand models for recovering angles created at the links of the hand [36, 37, 38]. The hand gesture is then estimated based on the relations between the 3D model and the observed image features.

**4.2.5 Motion**

Motion is a dynamic feature employed by some procedures for hand detection. Motion based recognition requires a highly controlled arrangement, and it adopts that the only movement in the image resulted from hand motion. In the case of fix cameras, the issue of movement assessment is solved with background maintenance and successive removal. This explanation is employed in [50,51] for recognizing the hand from other skin- coloured objects, and for testing with lighting conditions resulting from coloured lights. The difference in pixel strength between two consecutive frames is close to zero for the background pixels. Motion objects are placed by selecting and maintaining a suitable threshold.

**4.3 My Approach for Hand Detection**

 I propose an integrated system for detection, segmentation, and tracking of the hand in a gesture recognition system using a single webcam. Some other methods that use colour gloves [39, 40], my method can detect the plain hand posture by integrating two useful features: skin colour detection and contour matching. My proposed hand posture, finding algorithm has real-time performance and is strong against rotations, scaling, a cluttered background, and lighting conditions. Section 4.4.2 shows the strength of my proposed hand posture detection algorithm based on comparison with other different methods. Detecting the human hand in a plain background will boost the performance of hand gesture recognition systems. In this method, the speed and result of recognition will be the same for any frame size taken from a webcam such as 640×480, 320×240 or 160×120 and the system will be also robust against a plain background because I process the detected hand posture area only. A smaller image size that holds the detected hand posture area only must be like the training image size of a training stage as I will discuss the training and testing recognition systems stages in section.

 To detect the hand gesture in the image, a four-phase system was designed according to my approach and as shown in Figure 4.1. First, we will open camera which has square box to capture hand gesture. Second Put your hand in those boxes and make sure your hand covers with in the square box. Third, the skin colour locus for the image was removed from the user’s skin colour after face deletion. Then the last step, the hand gesture was spotted by removing false positive skin pixels and identifying hand gesture and other real skin colour regions using contours matching with the loaded hand gesture pattern contours. Skin Recognition Area Loading Hand Postures Patterns Contours Face Detection and Subtraction Capturing Images from Webcam or Video file Templates Contours Comparison with Skin Area Figure 4.1: Hand posture detection steps

**Figure 4.1 Hand posture detection steps**

**4.3.1 Skin Detection**

Skin detection is a useful approach for many computer vision applications such as face recognition, tracking and facial expression, abstraction, or hand tracking and gesture recognition.There are recognized procedures for skin colour modelling and recognition that will allow to differentiate between skin and non-skin pixels based on their colour**.**To get suitable distinction between skin and non-skin areas, a colour transformation is needed to separate luminance from chrominance [42].

The input images normally are in Colour format (RBG), which has the drawback of having components dependent on the lighting situations.The misunderstanding between skin and non-skin pixels can be decreased using colour space transformation**.**There are different approaches to detection skin colour components in other colour spaces, such as HSV, YCbCr, TSL or YIQ to provide better results in parameter recovery under changes in lighting condition. Researches have shown that skin colours of individuals cluster closely in the colour space for all people from different societies, for example, colour appearances in human faces and hands vary more in intensity than in chrominance [41, 43].Thus, take away the intensity V of the original colour space and working in the chromatic colour space (H, S) provides invariance against illumination situations. In [42], it had been well-known that removal the Value (V) component and only using the Hue and Saturation components, can still permit for the detection 96.83% of the skin pixels.In my application, I use the hue, saturation, value (HSV) colour model since it has shown to be one of the most adapted to skin-color detection [44].It is also well-matched with the human colour perception. In addition, it has real-time execution and it is more robust in cases of rotations, scaling, cluttered background, and changes in lighting condition.So, my projected hand gesture detection algorithm is real-time and robust against the mentioned previous changes.The other skin like objects existing in the image are removed from contour comparable with the loaded hand postures prototype contours**.**

The HSV colour space is gained by a nonlinear transformation of the essential RGB colour space.The conversion between RGB and HSV was described in [45].Hue (H) is a section that characterizes a pure colour such as pure yellow, orange or red, whereas saturation (S) provides a measure of the degree to which a pure colour diluted by white light [46]. Value (V) attempts to represent brightness along the grey axis such as white to black, but since brightness is subjective, it is thus difficult to measure [46].

According to [47] and Figure 4.2, Hue is estimated in HSV colour space by a position with Red starting at 0, Green at 120 and Blue at 240 degrees.The black mark in the diagram at the lower left on the screen determines the hue angle.

Saturation is a ratio that ranges between 0.0 along the middle line of the cone (the V axis) to 1 on the edge of the cone.Value ranges, string from 0.0 (dark) to 1.0 (bright).



**Figure 4.2 HSV Colour Space [47]**

According to [41],the HSV model can be resulting from non-linear transformation from an RGB model according to the following calculations.



4.1

4.2

4.4

4.3

As per a classification point of view, skin-color detection divided into two class problem: skin-pixel vs non-skin-pixel classification. Currently, there are different known classification approaches exits such as thresholding, Gaussian classifier, and multilayer perceptron [48, 52, 53].

In my research, I used a thresholding technique that allows getting a good result for higher computation speed when compared with other techniques, given our real-time requirements. This thresholding classification is used to find the values between two components H and S in the HSV model as I removed the Value (V) component. Usually, a pixel can be observed as being a skin-pixel when the following threshold values are synchronized satisfied: 0° < H < 20° and 75° < S < 190°.

**4.3.2 Contour Comparisons**

Once the skin colour has been detected, the contours of the detected skin colour are recovered and then compared them with the contours of the hand gesture patterns. Once skin colour contours are recognized as belonging to the hand gesture contour patterns, that area will be identified as a region of interest (ROI) which will then be used for tracking the hand movements and saving the hand posture in JPEG format in small images as shown in Figure 4.3. After that stored images will further be used to extract the features needed to recognize the hand postures in the testing stage.

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |

**Figure 4.3: Images of detected hand postures.**

If there is both hand gesture in the image, my system will substitute in detecting one of the two hands for every frame captured because the Open Computer vision function cvBoundingRect will circle one rectangle only around the detected hand, which has the main matching contours with the overloaded hand posture templates contours. The single frame will circle the detected hand posture for one frame and may enclose the other hand posture for the next frame if it has a higher matching contour.

**Chapter 5**

**Machine Learning Approach**

**5.1 Artificial Intelligence**

Research in Artificial Intelligence (AI) is very general and spawns across numerous different area such as mathematics, computer science, philosophy, economics and even ethics. This field is very wide and can be attempted from many different viewpoints. Therefore, this explanation will not be very exhaustive. For comprehensive and more complex joint into subject refer to [54].

One of many possible definitions of AI can be brief as a search to develop an artificial intelligent agent. In other words, it is an effort to create intelligent machines that are either intelligent or can be perceived as intelligent ones. One of the most important skills of intelligent agents is the sense of vision. Sense of vision is usually required to positive degree and not always it is necessary that it rivals the abilities of human visual apparatus.

First tries to resolve the vision problems were tackled from so called bottom-up approach in which the system was instructed with hard-coded set of protocol describing the vision. It was expected that as the understanding of a instruments allowing humans to abstract information from visual scene, the hard-coded systems can be fed this understanding and thus more skilled systems can be created. Problem with this method was that it highly underestimated the difficulty of reinforcement of these protocols. Therefore, it mainly failed to devise such a system.

This main idea the investigators to postulating that in order to resolve the problem of deploying vision capabilities for artificial intelligent system, it is compulsory to introduce a procedure that would allow AI systems to extract patterns from provided data. It is an overview of systems that can learn. Process that enables systems to learn is usually called machine learning.

Machine learning is again relatively extensive term that can be used in multiple different frameworks. In this work, it is meant to be understood as technique that is used to create mathematical representations used for image detection. There are numerous types of machine learning models that are useful for different tasks. The task that is conversed in this work and is also arguably most commonly attempted is called classification, which is the task to classify occurrence of input into correct discreet and mainly predetermined class. One more common type of machine learning task is called regression, which is based on the input data trying to estimation unknown continues valued quantity.

Rest of this document will be exclusively dealing with learning tasks of classification type.

**5.2 Image Processing**

Computer vision is important topic in image processing. Investigation in the subject was approaching the problem from bottom-up perception for many years. This was the before-mentioned effort to validate directions guiding the vision of living organisms. This method was actually very successful in certain environments.

General explanation of computer vision in image processing can be brief in following steps:

• Image capture - Image is captured using camera or similar device and digitized.

• Pre-processing - Captured image is modified to highlight important features such as noise reduction, contrast normalization etc.

• Segmentation detection - Selection of region of interest like edges, similar surfaces.

• Description – Feature extraction of radiometric, photometric descriptors and so on.

• Classification - Some means to categorize the object.



Figure 5.1: Diagram of image processing pipeline. [55]

Specific steps are shown in figure 5.1. Even though machine learning been as field of study since the second half of the 20th century, there was no wider implementation of its techniques in image processing for very long time. It was first announced in the classification step of the processing pipeline. In other words, complex difficulties were simplified by reducing the visual information contained within the image into handful of simple features that were nourished into machine learning model. This method consequently favours very simple models such as K-nearest Neighbours (KNN) or Support Vector Machines (SVM).

This carries the problem that these applications are not very useful. Each application is usually only capable of resolving very narrow problem and any deviation from ideal circumstances can mean failure. Application can have complications with varying contrast, brightness, scaling, rotation etc.

Second problem is often the fact that because image must be pre-processed numerous times before it is fed into machine learning model it requires additional time and computation resources. This is less of a problem with existing hardware innovations, but it is still not unimportant factor and it can have negative effect on the cost of the result. This is where machine learning in general indicates noteworthy advantage.

Conventional approach to computer vision can find success in applications that are deployed in very limited environments with rigid constraints. In controlled location, it is usually very simple to define the problem in formal guidelines. Even though it can be still available in certain places, it starts to be forced out by application of machine learning simply because the barrier of entry for extensive adoption reductions every day.

**5.3 Machine Learning**

As before described, Machine Learning is a process that is used to create models that can abstract information from data to resolve given problem and consequently repeatedly improves their performance.

Interesting viewpoint that can be used is to view machine learning as form of information compression. Where machine learning model is trying to abstract information from input data in such a way that the amount of a data used to save is summary while the information contained within is preserved.

**5.3.1 Machine Learning Approach**

There are mainly two different types of machine learning methods:

• Unsupervised Learning

• Supervised Learning

Both are mainly used for different types of machine learning tasks.

**Unsupervised learning**

In unsupervised learning method, the model is training by detecting new data and take out patterns in the date without being instructed on what they are. Contrasting to supervised learning defined below, the benefit of this method is that the model is able to learn from data without supervision. This means that there is no need for input data to be explained, therefore it takes a smaller amount time and resources to deploy these models in practice.

The biggest difficulty of supervised learning method in real world applications is to obtain appropriate data. Appropriate data in this context means, data that were someway classified into different categories, which can be very boring and slow process. In some situation, the task itself avoids the usage of labelled data. Labelled data are impossible to find or don’t exist at all.

Mainstream of unsupervised learning procedures belong to group called clustering algorithms. These algorithms are cantered on the idea to analyse ordered clustering of data in input space to determine their relationship. This is achieved by the belief that data point clustering in input space are likely to exhibit like properties.

Illustrations of unsupervised learning models are:

• K-means -clustering model

• Self Organizing Maps (SOMs)

• Principal Component Analysis (PCA) - dimensionality reduction

Image classification usually does not depend on the use of unsupervised learning methods; therefore, the following writing describes only supervised learning methods.

**Supervised learning**

Supervised learning method is more commonly used. This method needs training data with specific format. Each instance must have assigned label. These labels make available supervision for the learning algorithm. Training process of supervised learning is constructed on the following principle. First, the training data are fed into the model to produce estimate of output. This estimate is compared to the assigned label of the training data in order to evaluation model error. Based on this error the learning algorithm alters model’s parameters in order to reduce it.

**5.3.2 Structure of Machine Learning Algorithm**

Although machine learning algorithms are various and are using different methods its structure can be generalized. Structure of nearly all machine learning algorithms can be defined as composition of the following components:

• Dataset description

• Model

• Cost function

• Optimization technique

Almost all supervised learning algorithms use the same Dataset description. The other three components can vary intensely. This level of analysis is suitable for building of intuition for Neural Networks (NNs) and description of its individual components.

**Dataset description**

Supervised learning requires datasets with detailed properties. Each dataset holds set of 𝑛 instances which contains of a pair of input vector 𝑥𝑖 and output scalar 𝑦𝑖. Input vector

(5.1)

where 𝑖 is index of instance, 𝑝, is length of input vector.

Specific components of input vector must be of unified type. In case of image as input data it is value for individual pixels (e.g. 0-255). In other cases, they could be real values. Almost commonly in machine learning it stands that input should be normalized. This belief holds in images automatically since each pixel must have its vales in fixed range. It is very significant in other types of machine learning tasks, where this is not guaranteed.

Output scalar 𝑦𝑖 characterises class of given instance. Type of this output value thus must obtain only certain values. To put it differently, it must be a set of cardinalities equal to number of all possible classes.

**Model**

Model is prediction tackle that takes input 𝑥𝑖 to predict value of its output 𝑦𝑖. To each model has parameters represented by vector 𝜃, which are used to during the training process. The modest example of model type is linear model, also called linear regression. Parameters 𝜃 of this model are

, (5.2)

where 𝑝 is number of parameters equal to size of input vector 𝑥𝑖 . Prediction 𝑦^𝑖 of the model on instance 𝑖 is computed as

𝑦𝑖 = (5.3)

Therefore, estimates of the model on the entire dataset in matrix notation is

𝑦^ = 𝑋𝜃. (5.4)

Estimates in expanded notation are equal.

**Cost Function**

To achieve the learning skill of the machine learning algorithm, it is necessary to approximation the error of its predictions. This is assessed with so called cost function and called loss function.

This function must have certain properties. Ability of the machine learning algorithm to learn rests on the approximation of its improvement with change of its parameters. Therefore, cost function must be at least partially differentiable. In case of linear regression, it is most common to usage sum of square error. The main aim being that derivative of this function for linear model has only one global minimum.

Cost function is defined as

𝐽(𝜃) =(𝑦𝑖 − ^𝑦𝑖)2 = (︁𝑦𝑖 − 𝑥𝑖𝑇𝜃)︁ (5 . 6)

For the optimization determinations it is usually useful to express the cost function in matrix notation

𝐽(𝜃) = (𝑦 −𝑋𝜃)𝑇 (𝑦 −𝑋𝜃) (5.7)

**Optimization technique**

The last part of learning algorithm is the optimization technique. It consists of update of model’s parameters 𝜃 in order to progress its prediction. In other words, to find 𝜃 such that the value of cost function 𝐽(𝜃) for given dataset is as small as possible.

To examine the change of cost function on given dataset it is necessary to compute the derivative of 𝐽(𝜃) with respect to 𝜃

𝜕𝐽(𝜃)/𝜕𝜃= 𝜕/𝜕𝜃 [︁(𝑦 −𝑋𝜃)𝑇 (𝑦 −𝑋𝜃)]︁

= 𝜕/𝜕𝜃 [︁𝑦𝑇𝑦 + 𝜃𝑇𝑋𝑇𝑋𝜃 − 2𝑦𝑇𝑋𝜃]︁

= 2𝑋𝑇𝑋𝜃 − 2𝑋𝑇𝑦 (5.8)

For linear model is possible to find optimal result which is global minimum of the cost function. The optimal result

𝜃 =(︁𝑋𝑇𝑋)︁−1𝑋𝑇𝑦 (5.9)

is found by comparing the partial derivative of 𝐽(𝜃) to 0. Only condition is that 𝑋𝑇𝑋 must be non-singular.

Unfortunately, only very simple problems can be like using model as simple as linear regression. More complex model usually means more complex cost function. Optimization process of more complex cost functions cannot be definite to find global minimum. In this case, the optimization technique must be of iterative character. To put it in a dissimilar way, algorithm has to method the minimum of iterations. Many of the iterative approaches belong to the group called gradient based optimization.

**5.3.3 Model Complexity**

In the first calculation it could be said that the task of supervised machine learning is to model relationship between the input output data most correctly. The problem with this definition is that in the real-world application there is never enough data to capture true relationship between the two. Therefore, the task of machine learning is the attempt to suppose true relationship by detecting incomplete picture.

Hence the most significant property of machine learning model is its generalization capability. That is capability to produce meaningful outcomes from data that were not previously detected.

Generalization ability is reliant on complexity of the model and its relationship to complexity of underling problem. When model does not capture complexity of the problem appropriately it is defined as under fitting. In case the complexity of model surpasses the complexity of underling problem then this phenomenon is called over fitting.

In both extremes the generalization ability suffers. In the earlier case the model is unable to capture true intricacies of the problem and therefore is unable to predict wanted output reliably. In the last case it tries to capture even the subtlest data perturbation that might be in fact an outcome of stochastic nature of the problem and not the real underlying relationship. This can also cause the fact that input data is lost some variable necessary to capture the true relationship. This fact is unescapable, and it thus must be careful when designing machine learning model. Representation of this phenomena in case of two variable inputs is on Figure 5.2.



Figure 5.2: Figure shows different levels of generalization of model [56]

Typically, the machine learning model is trained on as much input data as possible in order to reach the best possible performance. At the same time its error rate must be verified on independent input data to checked whether the generalization ability is not deteriorating. This is typically accomplished by splitting available input data into training and testing set. Frequently in 4:1 fraction for training to test data. Model is trained with training data only and the presentation of the model is tested on the test data. Connection between test and train error can be found on Fig. 5.3. Even though the true generalization error can never be truly detected, its estimate by test error rate is enough for majority of machine learning tasks.

**Regularization**

Regularization is any alteration that is made to the learning algorithm that is intended to decrease its generalization error but not its training error [57]. As it has already been stated, the most significant aspect of machine learning is striking the stability between over and under fitting of the model. To support with this problem concept of regularization was devised. It is a method that helps to penalize the model for its complexity. Basic idea consists of adding a term in the cost function that increases with model complexity. When this is applied to cost function from equation 5.7

𝐽(𝜃) = (𝑦 −𝑋𝜃)𝑇 (𝑦 −𝑋𝜃) + 𝜆𝜃𝑇𝜃 (5.10)

where 𝜆 is a parameter that controls the strong point of the preference [57].



Figure 5.3: Relationship between the model complexity and its ultimate accuracy is the relationship between training and testing error [58].

**CHAPTER 6**

**NEURAL NETWORKS**

This chapter is dedicated to description of NN in general and its special type called CNN.

**6.1 History**

History of Neural networks can be arguably dated from 1943, when Warren Mcculloch and Walter Pitts invented mathematical model encouraged by the Biology of central nervous systems of mammals [59].

This encouraged the invention of Perceptron, created in 1958 by Frank Rosenblatt. Perceptron used very modest model mimicking biological neuron that was based on the mathematical model of Pitts and Mcculloch. Definition of the Perceptron model also defined an algorithm for direct learning from data.

In the beginning Perceptron looked very promising, but it was soon discovered that it had severe restrictions. Most projecting voices of criticism were Marvin Minsky. Minsky published book in which he laid out a case that the Perceptron model was unable to resolve complex problems [60]. Amongst others the book contained mathematical proof that Perceptron is incapable to solve simple XOR problem. More generally the Perceptron is only proficient of solving linearly separable problems. However, according to Minsky, this criticism wasn’t malicious, it in effect stifled the interest in NNs for over a period.

Awareness in NNs was rejuvenated in the early 80’s, when it was shown that any previously raised up deficiencies could have been resolved by usage of multiple units. This was later exacerbated by development of back-propagation learning algorithm, which allowed the possibility to gather neurons into groups called layers, which can be weighted into hierarchical structures to form a network. NN of this type were generally called Multilayer Perceptron (MLP). In 80s and 90s the awareness in NNs plateaued again and general research on AI was more focused on other machine learning methods. In the field of classification problems, it was particularly SVM and ensemble model. AI research communities also established several other paradigms of NNs that were likewise inspired by Biology of certain aspect of central nervous system but took different methods. Most significant examples were SOM and Recurrent Neural Network (RNN).

By the year 2000, there were very few research groups that were applying enough attention to the NNs. There was also certain disdain for NNs in the academic world and AI research community. The success of NNs that was promised almost half a century ago was finally coming across around 2009, when the first networks with huge number of hidden layers were effectively trained. This led to typical adaptation of umbrella term deep learning which by and large refers to Deep Neural Network (DNN). The term deep indicates that networks have many hidden layers

The key theoretic vision was to learn complex functions that could represent high-level abstractions such as vision recognition, language understanding, etc. There is a requirement for deep architecture.

NNs in the times before Deep Neural Networks had only one or two hidden layers. These are currently called shallow networks. Typical Deep Networks can have a number of hidden layers in order of 10’s, but in some cases even hundreds [61]

Still progress of Neural Network into the direction of structures with high number of hidden layers was obvious, its training was an unresolved technical problem for a very long time. There were fundamentally three reasons why this invention didn’t come sooner

1. There were no procedure allowing the number of hidden layers to measure.

2. There wasn’t enough of labelled data required to train the NN.

3. The computer hardware wasn’t powerful enough to train adequately large and complex networks successfully.

The first problem was tackled by the creation of CNNs [62]. The second problem was explained simply when there were more data presented. This was primarily achieved thanks to effort by large companies like YouTube, Google, Facebook, etc. But also, with support of large community of experts and hobbyists in data sciences.

Both inventions in computational hardware and improvement of training methods were needed to resolve the third problem. One of the technical revolutions was use of Graphics Processing Units (GPUs) for the demanding computation involved in the training of a complex network. Thanks to the fact that training process of NNs is typically large number of simple resulting computations, there is a great possibility for parallelization.

**6.2 Structure of Neural Networks**

The term NN is very general and it defines a comprehensive family of models. In this framework NN is distributed and parallel model that is capable of approximating complex nonlinear functions. Network is made from multiple computational components called neurons assembled topology.

Explanation of NN structure will follow the convention laid out in the explanation of learning algorithm. Meaning that an explanation of the learning algorithm is composed of model, cost function and optimization technique. The difference comes into performance with the fact that the model of NN is much more complex than the model linear regression. Therefore, the investigation is divided into model of neuron and topology of the network.

**6.2.1 Model of Neuron**

Neuron is computational unit carrying out nonlinear transformation of its inputs

𝑦 = 𝑔(𝑤𝑇𝑥 + 𝑏) (6.1)

Argument 𝑤𝑇𝑥 + 𝑏 of function 𝑔 is often observed as 𝑧. Therefore, the equation can be rewritten as

𝑦 = 𝑔(𝑧). (6.2)

Typical schema is shown on Figure 6.1, which describes inputs, weights bias and activation function.



Figure 6.1: Diagram of artificial neuron [63].

As it was already stated model of neuron was stimulated by biology. First attempts to make a model of a neuron had multiple elements equivalent with neurons of the human brain. As research proceeded this equality ceased being as important and modern NN models correspond to their biological matching part only superficially.

**Inputs**

Each neuron has multiple inputs 𝑥 that are combined to execute some operation. Each input has elected weight assigned to it.

**Weights**

Inputs of a neuron are weighted by parameters 𝑤 that are changed during the learning process. Each weight gives strength to each individual input into the neuron. The basic awareness is that when the weight is small the input doesn’t affect the output of the neuron very much. Its effect is large in the opposite case.

**Bias**

Another changeable parameter is bias 𝑏 that controls impact of the neuron.

**Activation Function**

For NN to estimate nonlinear function each neuron must perform the nonlinear transformation of its input. This is completed with activation function 𝑔 (𝑧) that performs the nonlinear transformation. There are numerous different normally used activation functions. Its usage depends on the type of network and on the type layer in which they activate.

One of the oldest and historically most frequently used activation functions if sigmoid function. It is defined by

𝑔(𝑧) = 1/1 + 𝑒−𝑧 (6.3)

Problem with sigmoid is that its gradient becomes flat on both extremes and as such it reduces the learning process [64].

One more activation function is hyperbolic tangent. It is defined as

𝑔(𝑧) = 𝑡𝑎𝑛ℎ(−𝑧). (6.4)

Hyperbolic tangent function is not use that much in feed forward NN, but it is mostly used in RNN. Currently most commonly used activation function is Restricted Linear Unit (ReLU). It is very generally used in both convolutional and fully connected layers. It is defined by

𝑔(𝑧) = max{0, 𝑧}. (6.5)

It has a disadvantage because it is not differentiable for 𝑧 = 0, but it is not a problem in software execution and one of its biggest advantages is that it can learn very speedily.

All three activation functions are illustrated in Figure 3.2.

**6.2.2 Topology of the Network**

There are several different generally used topologies. The two most frequently used in deep learning are feed-forward and recurrent. Feed forward networks are categorized by the fact that during activation the information move only in a forward direction from inputs to outputs. A recurrent network has some sort of feedback loop.

Another principle of topology is how are individual neurons in the network linked. Most commonly are NNs ordered in layers. In each layer there can be from one to n neurons. Layers are hierarchically fixed.  The first layer is called input layer, the last layer is called an output layer and the layers intermediate are called hidden.

Description of the network recreations on interconnections between individual layers. The most common structure is called fully connected where to each neuron in hidden layer 𝑙 has input associates from all neurons from previous layer 𝑙 − 1 and its output is associated with input of each neuron in following 𝑙 + 1 layer. The entire structure is illustrated in Figure 6.3.



Figure 6.2: Activation Functions

After this point on the term NN will refer to Feed-forward Fully Connected Neural Network.

Types of neurons are dependent on the type of the layer. Currently the core difference is in their activation function, which wasn’t the case for a long time. In history all layers had neurons with sigmoid activation function. It was mostly because the output sigmoid layer can be easily mapped onto probability distribution, since it obtains values between 0 and 1. Only relatively recently it was found that network composed of neurons with ReLU activation function in the hidden layers can be trained very speedily and are more resistant against over-fitting. Activation functions are still subject of ongoing research.

Neurons in output layer necessity output that can produce probability distribution



Figure 6.3: Fully connected Feed Forward Neural Network [65].

that can be used for approximation the probability of individual classes. For this reason, most frequently used activation function of output neuron is called SoftMax.

SoftMax is standardized exponential function. It is used to represent probability of an instance existence member of class 𝑗 as

(6.6)

where 𝐾 is total number of classes.

**6.2.3 Cost Function**

Cost functions of NNs are a complex subject that exceeds the scope of this thesis. One of the most common cost functions used in NNs for classification in multiple classes is categorical cross entropy. For SoftMax activation function from Equation 6.6 is a cost function defined as

where 𝑦 (𝑖) if correct class of the instance and 𝑛 is total number of instances.

**6.2.4 Optimization Procedure**

Every optimization technique for NN is constructed on gradient descent. In other words, it is an iterative process that goes to lower training error of the network by differentiating of the cost function and adjusting parameters 𝜃 of the model by following the negative gradient.

The problem is that cost function of the whole network is very complex and has many parameters. To find the gradient of the cost function, it is compulsory to go through all the units in the network and estimate their contribution to the overall error. A method that is used to solve this problem is called back-propagation.

Back-propagation if frequently confused to be a complete learning algorithm which is not the case, it is only the method to compute the gradient [57].

**Back-propagation**

To approximation the influence of individual units in a network the back-propagation is used to compute delta 𝛿 𝑙 𝑗 , where 𝑙 is layer and 𝑗 is index of neuron in that layer. Algorithm starts at the output of NN, more exactly its cost function.

*𝛿𝐿* = ∇*𝑥𝐶* ⊙ *𝑔'*′() (6.8)

where 𝐿 is last layer of the network and ∇𝑥𝐶 is gradient of cost function with respect to 𝑥 and ⊙ is the Hadamard product.

In subsequent lower layers the deltas are calculated as

where (𝑤𝑙+1) 𝑇 is from Equation 6.1.

Each neuron has two changeable parameters 𝑏 and 𝑤. To estimation the rate of change for parameter 𝑏 𝑙 𝑗 from Equation 6.1 it needs to be computed as

(6.10)

Change of weight 𝑤 𝑙 𝑗𝑘 from Equation 6.1 it needs to be computed as

(6.11)

**Gradient Descent Optimization**

Back-propagation estimations gradient of all modifiable parameters 𝑏 and 𝑤 in the network. These parameters can be denoted by vector 𝜃. Therefore, the gradient of the function to be minimized can be written as ∇𝜃𝑡−1 𝑓(𝜃𝑡−1).

Modest learning algorithm is called gradient descent. Even though simple, it is very robust learning algorithm.

(6.12)

(6.13)

Algorithm has meta-parameter 𝜂, which is often called learning rate. It determines how fast are 𝜃 parameters updated. Modest gradient descent has the shortcoming that update of parameters is always closely proportional to change of gradient. This might turn out to be a problem when the gradient change slows down. This process is also often called Stochastic Gradient Descent (SGD). The word stochastic indicates that during training the algorithm is using random choice of instances to train. There are various variations on the gradient descent method. Following explanations are taken from [66].

**Adam**

It is more complex learning algorithm that combines 𝐿2 norm and classical momentum-based optimization. It should converge quicker than classical Gradient Descent.

)

(6.16)

**6.3 Convolutional Neural Networks**

CNNs are specialized type of NNs that was initially used in image processing applications. They are arguably most effective models in AI inspired in biology.

Even though they were shown by many different fields, the main design principles were drawn from neuroscience. Since their achievement in image processing, they were also very successfully implemented in nature language and video processing application.

A fore mentioned stimulation in biology was based on scientific work of David Hubel and Torsten Wiesel. Neurophysiologists Hubel and Wisel, studied vision system of mammals from late 1950 for several years. In the research, that might be measured little gruesome for today’s standards, they linked electrodes into brain of anesthetized cat and measured brain response to visual stimuli [67]. They discovered that feedback of neurons in visual cortex was triggered by very narrow line of light shined under specific angle on projection screen for cat to see. They determined that specific neurons from visual cortex are responding only to very specific patterns in input image. Hubel and Wiesel were given the Nobel Prize in Physiology and Medicine in 1981 for their discovery.

In the following text is assumed that convolutional layer is working with rectangular input data (e.g. images). Even though the Convolutional networks can also be also used to classify one-dimensional or three-dimensional input.

**6.3.1 Structure of CNN**

Structure of Convolutional networks is typically made of three different types of layers. Layer could be either Convolutional, Pooling or fully connected. Each type of layer has different protocol for forward and error backward signal propagation.



Figure 6.4: Structure of Convolutional Neural Network [68]

There are no specific protocols on how the structure of individual layers should be organized. However, with exemption of recent development CNNs are typically structured in two parts. First portion, usually called feature extraction, is using groupings of convolutional and pooling layers. Second portion called classification is using fully connected layers. This is shown in Figure 6.4.

**Convolutional layer**

As the name suggests this layer employs convolution procedure. Parameters supply to this layer is simply called input. Convolution process is performed on input with specific filter, which is called kernel. Output of convolution process is typically called feature map.

Input into Convolutional layer can be image or feature map from previous layer. Kernel is typically of rectangular shape and its width can array from 3 to N pixels. Feature map is created by convolution of kernel over each definite element of input. Convolution is defined in more detail in section describing training of CNN.

Depending on the dimensions of kernel and layer’s padding preferences the process of convolution can produce feature map of different size than input. When the size of output should be preserved it is compulsory to employ zero padding on the edges of input. Zero padding in this case must add essential amount of zero elements around the edges of input. This amount is determined by

p =((h−1)/2) (6.19)

where h is width of used kernel. In contrary case the feature map is reduced by the 2p. Decrease of size of the feature map can be in some cases desirable. Zero padding is shown on Figure 6.5.

Drop of feature map can go even further in case of use of stride. Application of stride specifies by how many input points is navigated when moving to neighbouring position in each step. When the stride is one, kernel is moved by one on each step and the resulting size of feature map is not affected. Each Convolutional layer is typically configuration of several different kernels. In other words, output of this layer is tensor holding feature map for each used kernel. Each of these is premeditated to underline different features of input image. In the first layers these features are typically edges. next the layer, the more complex features are captured. Each kernel that is used is applied to all inputs of the image to produce one feature map which basically means that neighbouring layers are distribution the same weights. This might not be appropriate in some applications and therefore it is possible to use two other types of networks. Locally linked which basically means that applied kernel is of the same size as the input and smooth convolution which means alternation of more than one set of weights on entire input.



Figure 6.5: A zero padded 4x4 matrix [69]

Smooth convolution is interesting because with clever combination with Max Pooling clarified bellow it allows to train specific feature from multiple positions. Each convolutional layer has non-linearity on its output that is sometimes also called the detector phase. This is equal to activation function of NNs. Activation function of CNN is normally ReLU.

**Pooling layer**

This layer typically doesn’t find any learning process, but it is used to dejected sample size of the input. The Principle is that input is divided into multiple not overlapping rectangular elements and units within each element are used to make single unit of output. This reduce the size of output layer while preserving the most important information checked in input layer. In other words, pooling layer wrappings information contained within input. Type of process that is achieved on each element determines a type of pooling layer. This action can be averaging over units within element, selecting maximal value from element or alternatively learned linear combination of units within element. Learned linear combination introduces form of learning into the pooling layer, but it is not very predominant. Selecting of maximal value is record common type of pooling operation and in that case the layer is called Max-Pooling accordingly. Positive outcome of Max-pooling down-sampling is that take out features that are learned in convolution are invariant to small shift of input. Principle of Max-Pooling is shown on Figure 6.6.

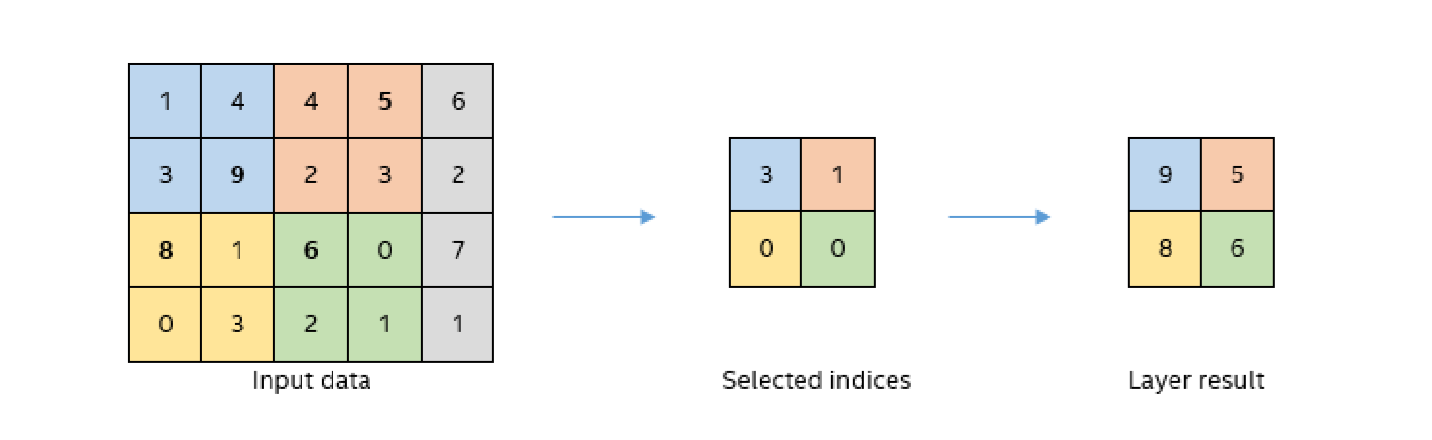


Figure 6.6: Principle of Max-pooling [70]

As already said, another benefit of Max-pooling arises when combined with tiled convolution. To generate simple detector that is invariant to rotation it possible to use four different kernels that are rotated by 90 degrees among each other and when the smooth convolution is used to tile them in groups of four, the Max-pooling makes sure that resulted feature map holds output from the kernel with strongest signal. Max-Pooling layer will be used to define process of training of CNNs.

**Fully-Connected layer**

Fully-Connected layer is equal to layer from Fully Connected Neural Network (FCNN) that was already described. Its training also follows already described procedure.

**6.3.2 Training of CNN**

Optimization procedure of CNN is similarities to FCNN. Situation with CNN is more complex because network is made of different types of layers. Forward signal propagation and backward error propagation are following special protocol for each layer. Calculations used in this section were inspired from [73]. First stage is called forward-propagation, where the signal is broadcast from inputs of the CNNs to its output. In the last layer the output is associated with desired value by cost function and error is estimated. In second stage is again used backpropagation algorithm to estimate error contribution of individual units. Inconstant parameters of the network are again optimization by gradient descent algorithm.

**Forward Propagation of Convolution Layer**

Each convolutional layer is preforming convolution process on its input. Presuming that input of a layer is of length N × N units and kernel is of length m × m. Convolution is calculated over (N−m+1)×(N−m+1) units without zero padding.

Calculation of convolution output xlij is defined as0

where is index of current layer, ωab are weights of the kernel and is output of previous layer. Output of convolutional layer is computed by squashing of output of convolution operation through non-linearity:

where g represents this non-linear function.

**Backward Propagation of Convolution Layer**

Backward propagation for convolutional layer is following the similar principles as described in Section 6.2.4. The difference is in fact that convolution kernel shares weights for entire layer and kernels do not have bias described in Section 6.2.1. Given partial derivative of error from previous layer with respect to output of convolutional layer , influence of kernel weights on the cost function it needs to calculate

From Equation 6.20 it follows that ,thus

To calculate deltas (equivalent to Equation 6.9) using the chain rule

=

Since is already given the deltas is calculated by derivation of activation function. Last phase comes to propagation of error into previous layer by equation

Again, from Equation 6.29 it follows that =ωab, therefore

The result looks suspiciously like convolution operation and can be taken as convolution of error with flipped kernel.

**Forward Propagation of Pooling layer**

Feed forward operation of pooling layer is strait forward as defined in section 6.3.1. Ratio is typically four to one, which means that input matrix is divided into not overlapping sub-matrices of size 2×2 and each of these produces 1 output. Another possibility is to have overlapping sub-matrices, where length of sub-matrix is larger the number of pixels between application of pooling.

**Backward Propagation of Pooling Layer**

As said in section for forward-propagation, there is no explicit learning process happening in pooling layer. Error is propagated backwards dependent on how the signal was propagated forward. In Max-Pooling layer the error is propagated only to the unit with maximal output in forward-propagation phase. The error is propagated very sparsely, as outcome.

**6.4 Regularization of Neural Networks**

Control of difficulty applies to both NN and CNN. There are several popular regularization techniques that typically consist of adjustment of cost function or optimization algorithm. Somewhat different approach is to modify structure of the network during training stage.

Dropout By far the greatest regularization technique is to combine predictions of many different models. This technique greatly improves generalization ability of combined model while preventing over-fitting. Exactly on this idea are based ensemble models. The problem with ensemble models is that they are required more computational time and very expensive. Because of this, ensembles are usually made of many very simple models [71]. This idea is especially problematic with DNNs, which are model with many parameters that are difficult to train. Moreover, even when trained models are existing in some applications it still isn’t viable to evaluate many different models in production environment. Another problem is that there might not be enough data to train these different models.

All these problems can be resolved by dropout technique. The basic idea is that each neuron in the network has certain probability to be deactivated during one iteration. This potential for deactivation is estimated in every iteration, to ensure that network has different architecture every time. Deactivated means that it will not broadcast any signal through. This forces individual neurons to pick up features that are less dependent on its surrounding.

Possibility for deactivation is a hyper-parameter that can be tuned, but reasonable default value is 0.5. Dropping out is only happening in the training stage. In testing stage are all weight connection multiplied by the probability of a dropout. This is completed because the activation of the network must stay roughly equivalent in both training ant testing stage. Basic concept is shown in Figure 6.7

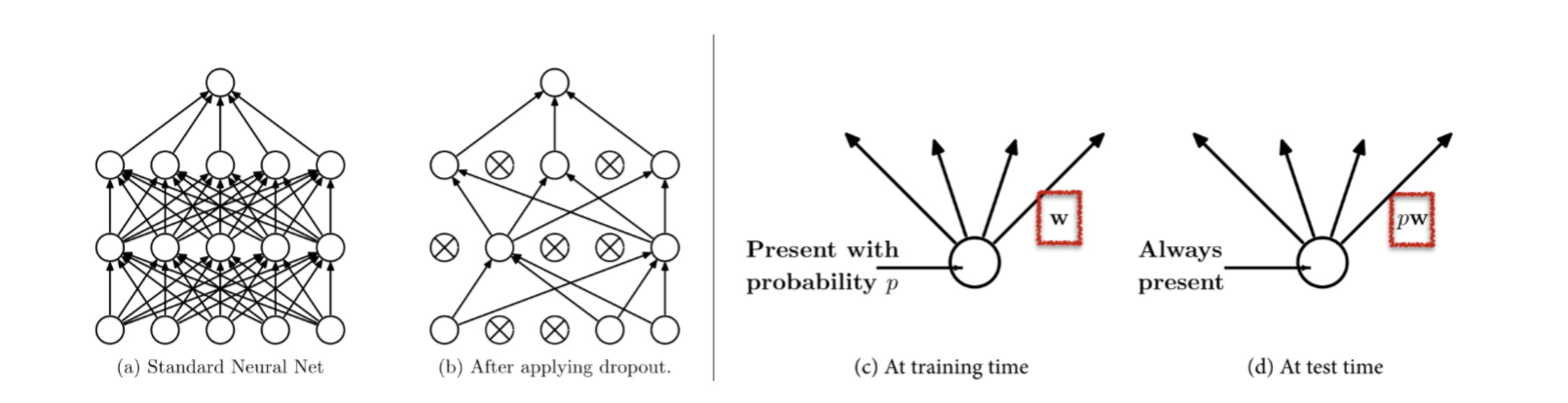


Figure 6.7: Dropout: (a)Standard fully connected network. (b) Network with some neurons deactivated. (c) Activation of neuron during training phase. (d) Activation of neuron during testing phase [72].